# The $\mathrm{C}_{3}$-bending vibrational levels of the $\mathrm{C}_{3}-\mathrm{Kr}$ and $\mathrm{C}_{3}-\mathrm{Xe}$ van der Waals complexes studied by their $\tilde{\mathbf{A}}-\tilde{\mathbf{X}}$ electronic transitions and by ab initio calculations 

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#### Abstract

Fluorescence excitation spectra and wavelength-resolved emission spectra of the $\mathrm{C}_{3}-\mathrm{Kr}$ and $\mathrm{C}_{3}-\mathrm{Xe}$ van der Waals (vdW) complexes have been recorded near the $2^{2-}{ }_{0}, 2^{2+}{ }_{0}, 2^{4-}{ }_{0}$, and $1^{1}{ }_{0}$ bands of the $\tilde{\mathrm{A}}^{1} \Pi_{u}-\tilde{\mathrm{X}}^{1} \Sigma_{\mathrm{g}}^{+}$system of the $\mathrm{C}_{3}$ molecule. In the excitation spectra, the spectral features of the two complexes are red-shifted relative to those of free $\mathrm{C}_{3}$ by $21.9-38.2$ and $34.3-36.1 \mathrm{~cm}^{-1}$, respectively. The emission spectra from the $\tilde{\mathrm{A}}$ state of the Kr complex consist of progressions in the two $\mathrm{C}_{3}-$ bending vibrations ( $\nu_{2}, \nu_{4}$ ), the vdW stretching ( $\nu_{3}$ ), and bending vibrations ( $\nu_{6}$ ), suggesting that the equilibrium geometry in the $\tilde{\mathrm{X}}$ state is nonlinear. As in the Ar complex [Zhang et al., J. Chem. Phys. 120, 3189 (2004)], the $\mathrm{C}_{3}$-bending vibrational levels of the Kr complex shift progressively to lower energy with respect to those of free $\mathrm{C}_{3}$ as the bending quantum number increases. Their vibrational structures could be modeled as perturbed harmonic oscillators, with the dipole-induced dipole terms of the Ar and Kr complexes scaled roughly by the polarizabilities of the Ar and Kr atoms. Emission spectra of the Xe complex, excited near the $\tilde{A}, 2^{2-}$ level of free $\mathrm{C}_{3}$, consist only of progressions in even quanta of the $\mathrm{C}_{3}$-bending and vdW modes, implying that the geometry in the higher vibrational levels ( $v_{\text {bend }} \geq 4, \mathrm{E}_{\text {vib }} \geq 328 \mathrm{~cm}^{-1}$ ) of the $\tilde{\mathrm{X}}$ state is (vibrationally averaged) linear. In this structure the Xe atom bonds to one of the terminal carbons nearly along the inertial $a$-axis of bent $\mathrm{C}_{3}$. Our $a b$ initio calculations of the Xe complex at the level of $\operatorname{CCSD}(\mathrm{T}) /$ aug-cc-pVTZ (C) and aug-cc-pVTZPP ( Xe ) predict that its equilibrium geometry is T -shaped (as in the Ar and Kr complexes), and also support the assignment of a stable linear isomer when the amplitude of the $\mathrm{C}_{3}$ bending vibration is large ( $v_{4} \geq 4$ ). © 2011 American Institute of Physics. [doi:10.1063/1.3506635]


## I. INTRODUCTION

The van der Waals (vdW) complexes of rare-gas ( Rg ) atoms with various molecules have been studied extensively. Where the complexes are T-shaped, it has been found that as the rare gas atom varies from Ne to Xe , the vdW bond lengths and bond angles change only slightly. This happens partly because the increasing atomic radius of the Rg atom compensates for some of its increasing polarizability, ${ }^{1}$ and partly because the vdW bond length is greater than the sum of the atomic radii. ${ }^{2}$ Although the vdW bond lengths of the $\mathrm{Rg}-\mathrm{CO}$ complexes change very little as the atomic number of the Rg atom increases, the bond angle becomes more nearly $90^{\circ}$. ${ }^{\text {T }}$ The anisotropy of the angular potential for T-shaped complexes is expected to be greater for Xe than for other Rg atoms. Since the atomic radius of Xe is comparatively large and the binding energy is greatest for Xe complexes, a small angle deviation from the equilibrium geometry of a Xe complex will cause its energy to rise rapidly. Similar phenom-
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ena have been reported for non-T-shaped complexes, such as $\mathrm{Xe}-\mathrm{H}_{2}$ (Ref. 3) and $\mathrm{Xe}-\mathrm{CH}_{4} .{ }^{4}$

By contrast, certain rare gas complexes exist in isomeric forms. Isomers occur for He and Ne complexes because of their weak vdW bonds and small angular anisotropy. The vibrational amplitudes are often large in such complexes, which makes their geometry determinations difficult. ${ }^{5}$ As for complexes with heavier rare gas atoms, both linear (L-) and Tshaped isomers have been reported for $\mathrm{Ar}-\mathrm{I}_{2}$ (Refs. 6 and 7) and $\mathrm{Ar}-\mathrm{Br}_{2}{ }^{8,9}$ Although the two isomers of $\mathrm{Ar}-\mathrm{Br}_{2}$ are energetically nearly degenerate, the lines in the optical spectra of the T-shaped isomer are sharp ${ }^{8}$ while those of the linear isomer are diffuse ${ }^{9}$ as a result of a bound-to-free transition. The spectroscopic characterizations of the isomers of other Rgmolecule complexes could be useful in understanding matrix isolation spectroscopy.

Wavelength-resolved emission spectra from the Ã state of the $\mathrm{C}_{3}-A r$ complex have previously allowed us to map the $\mathrm{C}_{3}$ bending vibrational levels of its ground electronic state. ${ }^{10}$ The results showed that the level structure can be modeled as a harmonic oscillator perturbed by a dipole-induced dipole interaction potential. ${ }^{10}$ As the $\mathrm{C}_{3}$ molecule bends away from its linear configuration its dipole moment increases, which has the effect of stabilizing the Ar complex, and lowering its levels
relative to those of free $\mathrm{C}_{3}$ by as much as $82 \mathrm{~cm}^{-1}$ at $v_{\mathrm{b}}=10$. The observed $\mathrm{C}_{3}$-bending vibrational levels of the Ar complex were assigned as the progression $v_{2 \text {, in-plane }}=1, v_{4 \text {, out-of-plane }}$ $=v_{\mathrm{b}}-1,\left(v_{\mathrm{b}}=v_{2}+v_{4} \geq 2\right)$, consistent with the near-Tshaped equilibrium geometry predicted by our ab initio calculation. No linear isomer was found. Wavelength-resolved emission spectra of the Ar complex therefore allowed us to study higher bending levels of the vdW complex, ( $v_{\mathrm{b}} \geq 4$ ), which would not be observable in microwave and infrared experiments, where only the lowest levels can be seen.

One of the aims of the present work is to test whether our perturbed harmonic oscillator ( $\mathrm{PHO} \mathrm{)} \mathrm{model} \mathrm{for} \mathrm{the} \mathrm{Ar} \mathrm{com-}$ plex can be extended to the Kr and Xe complexes. The results provide experimental evidence that the geometries of both the $\tilde{\mathrm{X}}$ and $\tilde{\mathrm{A}}$ states of the Kr complex are T-shaped (like those of the Ar complex), and that our PHO model works well for the $\mathrm{C}_{3}$-bending vibrational levels of its ground electronic state. To our surprise, wavelength-resolved fluorescence spectra of the Xe complex indicate the existence of an L-isomer at $v_{\mathrm{b}} \geq 4$. The potential energy surfaces of the Ar and Xe complexes calculated in our previous work ${ }^{10}$ and this work give the relative stabilities of the L-isomers of these two complexes.

## II. EXPERIMENTAL DETAILS

Two different types of nozzle were used in this work: a home-made slit nozzle ( $2 \mathrm{~mm} \times 50 \mu \mathrm{~m}$ ) and a circular nozzle with a $500 \mu \mathrm{~m}$ diameter. The slit nozzle was used for collecting emissions from weak vdW transitions and for reducing the Doppler width of the excitation spectra. The gas mixture used for generating the Kr and Xe complexes was $0.03 \%-0.06 \%$ of allene, $4 \%$ of Kr or Xe , with a balance of 50:50 He :Ne gas mixture. To eliminate the possibility of interference by the Ne complex, which might be formed at this high Ne concentration, some experiments with the Xe complex were carried out using pure He instead of the $50: 50 \mathrm{He}: \mathrm{Ne}$ mixture. Lower concentrations ( $0.03 \%$ ) of allene were used when it was necessary to reduce the internal energy of the vdW complex. The backing pressure was typically about 5.3 atm .

The gas mixture was photolysed by radiation from an ArF (193 nm) excimer laser (Lambda Physik, LPX 110i), aligned so as to intersect the supersonic molecular beam near the tip of the nozzle orifice. Since it requires two 193 nm photons to dissociate allene to produce $\mathrm{C}_{3}$, the focusing has to be carried out carefully so as to minimize three-photon dissociation processes. Three-photon processes give translationally and rotationally hot $\mathrm{C}_{3}$ molecules, which lower the yield of the $\mathrm{C}_{3}-\mathrm{Rg}$ vdW complex.

The bands of the $\mathrm{C}_{3}-\mathrm{Rg}$ vdW complexes accompanying the $\tilde{A}^{1} \Pi_{u}-\tilde{X}^{1} \Sigma_{\mathrm{g}}^{+}$system of $\mathrm{C}_{3}$ were probed by laser-induced fluorescence (LIF) and wavelength-resolved emission methods. To obtain fluorescence excitation spectra of the Kr and Xe complexes, a tunable dye laser (Lumonics Inc. HD 500) was scanned in the range of $388-405 \mathrm{~nm}$. The LIF spectra were calibrated against simultaneously recorded optogalvanic spectra of an $\mathrm{Fe}-\mathrm{Ne}$ hollow cathode lamp. ${ }^{11}$ The relative frequencies reported here are accurate to at least $\pm 0.1 \mathrm{~cm}^{-1}$; however, the absolute frequencies appear to be
good only to $\pm 0.5 \mathrm{~cm}^{-1}$, comparing our measurements of the $\mathrm{C}_{3}$ bands with those reported in Refs. 12-14.

In the wavelength-resolved emission experiments, the fluorescence was dispersed by a 0.3-m-monochromator (Jobin-Yvon HR 30) with a 2400 lines $/ \mathrm{mm}$ grating. The slit width was set to $40-100 \mu \mathrm{~m}$, depending upon the fluorescence intensity of the band under study; the spectral resolution of the emission therefore ranges from 8.5 to $20 \mathrm{~cm}^{-1}$. Spectral calibration was carried out using emission lines from an $\mathrm{Fe}-$ Ne hollow cathode lamp. ${ }^{11}$ The absolute frequencies of the $\mathrm{C}_{3}$ emission lines agree to $\pm 2 \mathrm{~cm}^{-1}$ with the stimulated emission pumping measurements of Northrup and Sears. ${ }^{15}$ More details of the experimental conditions can be found elsewhere. ${ }^{10}$

## III. FLUORESCENCE EXCITATION SPECTRA OF THE $\mathrm{C}_{3}-\mathrm{Kr}$ AND $\mathrm{C}_{3}-\mathrm{Xe}$ vdW COMPLEXES

Fluorescence excitation spectra of the $\mathrm{C}_{3}-\mathrm{Kr}$ and $\mathrm{C}_{3}-\mathrm{Xe}$ complexes have been recorded near the $(0,0), 2^{2-}{ }_{0}$, $2^{2+}{ }_{0}, 2^{4-}{ }_{0}$, and $1^{1}{ }_{0}$ bands of the $\tilde{\mathrm{A}}^{1} \Pi_{\mathrm{u}}-\tilde{\mathrm{X}}^{1} \Sigma_{\mathrm{g}}^{+}$system of the $\mathrm{C}_{3}$ monomer. Figure 1 shows the excitation spectra of the Kr complex near these five bands. The $\mathrm{R}(0)$ lines of the various $\mathrm{C}_{3}$ bands in Fig. 1 have been aligned vertically in the panels. The excitation spectra of the Kr complex are very similar to those of the Ar complex; ${ }^{10}$ for instance, (i) no vdW band is observed near the $(0,0)$ band of $C_{3}$, (ii) vdW bands were observed both to the red (low-frequency side) and blue


FIG. 1. The fluorescence excitation spectra of the $\mathrm{C}_{3}-\mathrm{Kr}$ complex recorded near the $(0,0), 2^{2-}{ }_{0}, 2^{2+}{ }_{0}, 2^{4-}{ }_{0}$, and $1^{1}{ }_{1}$ bands of the Comet system of $\mathrm{C}_{3}$ under supersonic beam conditions. The spectral features marked with arrows were assigned to the Kr complex. The $\mathrm{R}(0)$ lines of the $\mathrm{C}_{3}$ bands in each panel have been lined up vertically. The low-frequency side of the excitation spectrum recorded near the $(0,0)$ band was shifted upwards and its intensity was enhanced by a factor of 5 to show that no Kr complex was observed.


FIG. 2. The fluorescence excitation spectra of the $\mathrm{C}_{3}-\mathrm{Xe}$ complex recorded near the $2^{2-}{ }_{0}, 2^{2+}{ }_{0}$, and $2^{4-}{ }_{0}$ bands of the Comet system of $C_{3}$ under supersonic beam conditions. Spectral features marked with arrows were assigned to the Xe complex.
(high-frequency side) of the transitions to vibrationally excited $\mathrm{C}_{3}(\tilde{\mathrm{~A}})$, (iii) vdW bands to the red of the $\mathrm{C}_{3}$ transitions are much more intense than those to the blue, (iv) the most intense vdW band is a doublet, and (v) the largest vdW shifts were observed near the $2^{2+}{ }_{0}$ and $2^{4-}{ }_{0}$ bands of the $C_{3}$ system.

For the Xe complex, again no band was found near the $(0,0)$ band of the $C_{3}$ system. Since there are strong singlettriplet perturbations in the zero-point level of the A state, ${ }^{12,16}$ it is quite probable that the zero-point level of the $\tilde{A}$ state of the $\mathrm{C}_{3}-\mathrm{Rg}$ complex undergoes fast vibrational predissociation from the triplet manifolds through the singlet-triplet mixed doorway states. ${ }^{10}$ The excitation spectra of the Xe complex near the $2^{2-}{ }_{0}, 2^{2+}$, and $2^{4-}{ }_{0}$ bands of $\mathrm{C}_{3}$ (shown in Fig. 2) have fewer progressions than those of the Ar and Kr complexes and bands were only observed to the red side of the $\mathrm{C}_{3}$ bands. Most of the Xe complex bands are too broad to show any evidence of doublet structure.

Table I lists the largest frequency shifts observed for the $\mathrm{Ar}, \mathrm{Kr}$, and Xe vdW complexes near the $2^{2-}{ }_{0}, 2^{2+}{ }_{0}$, and $2^{4-}{ }_{0}$ bands of free $\mathrm{C}_{3}$. These represent the amounts by which the $\mathrm{C}_{3}$-bending levels of the complexes are lowered relative to those of free $\mathrm{C}_{3}$. Near the $2^{2-}{ }_{0}$ band of $\mathrm{C}_{3}$, the observed vdW red-shifts simply follow the trend of the increasing polarizabilities of the $\mathrm{Ar}, \mathrm{Kr}$, and Xe atoms; this suggests that the $\tilde{\mathrm{A}}$, $2^{2-}$ level of $\mathrm{C}_{3}$ is only slightly perturbed by the nearby Rg atom. The orbital angular momentum of the $\tilde{\mathrm{A}}$ state ${ }^{17}$ of $\mathrm{C}_{3}$

TABLE I. Largest red-shifts $\left(\mathrm{cm}^{-1}\right)$ observed in the $\mathrm{C}_{3}-\mathrm{Ar}, \mathrm{C}_{3}-\mathrm{Kr}$, and $\mathrm{C}_{3}-$ Xe van der Waals complexes from the $\mathrm{R}(0)$ lines of the free $\mathrm{C}_{3}$ transitions.

|  | $2^{2-}{ }_{0}$ | $2^{2+}{ }_{0}$ | $2^{4-}{ }_{0}$ |
| :--- | :---: | :---: | :---: |
| Ar | 14.2 | 31.1 | 35.5 |
| Kr | 21.9 | 38.1 | 38.1 |
| Xe | 34.3 | 34.9 | 33.8 |

mixes the characters of the $2^{2+}$ and $2^{4-}$ levels quite strongly and also mixes them with higher bending levels. Since higher bending levels of $\mathrm{C}_{3}(\tilde{\mathrm{~A}})$ are expected to have larger dipole moments, the vdW bond in $\mathrm{C}_{3}$ ( $\tilde{\mathrm{A}}, 2^{2+}$ or $2^{4-}$ ) -Rg should be stronger than that in $\mathrm{C}_{3}\left(\tilde{\mathrm{~A}}, 2^{2-}\right)-\mathrm{Rg}$. This could explain the larger red-shifts observed in these two bands of the Ar and Kr complexes. However, the red-shifts of these three bands in the Xe complex seem to have reached a limiting value. Perhaps this limit arises from poorer Franck-Condon factors which prevent us from observing the full vdW progressions near the $2^{2+}{ }_{0}$ and $2^{4-}{ }_{0}$ bands of $\mathrm{C}_{3}$.


FIG. 3. Top figure: Excitation spectrum of $\mathrm{C}_{3}-\mathrm{Kr}$ near the $2^{2-}{ }_{0}$ band of free $\mathrm{C}_{3}$. Below are traces of the wavelength-resolved emission spectra obtained by exciting the blended $\mathrm{R}(0)$ and $\mathrm{Q}(2)$ lines of $\mathrm{C}_{3}$ and by exciting the Kr complex at the vdW bands labeled A-D, respectively.


FIG. 4. Top figure: Excitation spectrum of $\mathrm{C}_{3}-\mathrm{Kr}$ near the $2^{4-}{ }_{0}$ band of free $\mathrm{C}_{3}$. Below are traces of the wavelength-resolved emission spectra obtained by exciting the blended $R(0)$ and $Q(2)$ lines of $C_{3}$ and by exciting the Kr complex at the vdW bands labeled E-G, respectively.


FIG. 5. Top figure: Excitation spectrum of $\mathrm{C}_{3}-\mathrm{Kr}$ near the $1^{1}{ }_{0}$ band of free $\mathrm{C}_{3}$. Below are traces of the wavelength-resolved emission spectra obtained by exciting the blended $R(0)$ and $Q(2)$ lines of $C_{3}$ and by exciting the Kr complex at the vdW bands labeled $\mathrm{H}-\mathrm{K}$, respectively.

## IV. WAVELENGTH-RESOLVED EMISSION SPECTRA OF THE $\mathrm{C}_{3}-\mathrm{Kr}$ COMPLEX

Figures 3-5 illustrate wavelength-resolved emission spectra obtained by exciting free $\mathrm{C}_{3}$ or its Kr complex, at or near the $2^{2-}{ }_{0}, 2^{4-}{ }_{0}$, and $1^{1}{ }_{0}$ bands of $\mathrm{C}_{3}$. Each figure is in three parts. The top trace is the excitation spectrum, showing the bands of the Kr complex superimposed on the bands of free $\mathrm{C}_{3}$. Letters indicate the bands of the complex from which wavelength-resolved emission spectra (shown in the middle part of the figure) were recorded. At the bottom of the figure is the emission spectrum given by the $\mathrm{C}_{3}$ band itself. All the bands examined arise from the ground vibrational level of $\mathrm{C}_{3}$ or the Kr complex, so that the energies of the lower levels of the various emission features can be obtained directly, by subtracting the observed emission frequency from the excitation frequency. Fourteen bands of the Kr complex, observed near the $2^{2-}{ }_{0}, 2^{2+}{ }_{0}, 2^{4-}{ }_{0}$, and $1^{1}{ }_{0}$ bands of $\mathrm{C}_{3}$, have been studied by this dispersed fluorescence (DF) method. No emission was observed from free $\mathrm{C}_{3}$ itself, indicating that the $\tilde{A}$-state complex of this study is bound.

Some excitation bands of the Kr complex are much broader than the spectral resolution $\left(\sim 0.25 \mathrm{~cm}^{-1}\right)$ of our pulsed dye laser. For these broad vdW bands, such as those at 25017 and $25737 \mathrm{~cm}^{-1}$, we recorded more than one DF spectrum, setting the excitation laser to different parts of the broad profile. As shown in Fig. 5, where three close-lying excitation frequencies ( $25736.1,25737.0$, and $25738.0 \mathrm{~cm}^{-1}$ ) were chosen, it is seen that the emission spectrum obtained by exciting the Kr complex at $25736.1 \mathrm{~cm}^{-1}$ (labeled as H ) is quite different from the other two (labeled as I and J), suggesting that the broad feature is an unresolved blend of two, or possibly more, vdW bands. Table II lists the observed vibrational levels of the Kr complex up to $1000 \mathrm{~cm}^{-1}$ above its ground vibrational level. In this region only $\mathrm{C}_{3}$-bending, vdW stretching, and vdW bending vibrations are expected, since the stretching vibrations of free $\mathrm{C}_{3}$ lie above this energy. Following Ref. 10, we number the vibrational modes of the Kr complex assuming $\mathrm{C}_{2 \mathrm{v}}$ symmetry: $\nu_{1}$ and $\nu_{5}$ are the symmetric and antisymmetric $\mathrm{C}-\mathrm{C}$ stretching vibrations, $\nu_{2}$ $\left(\mathrm{a}_{1}\right)$ and $\nu_{4}\left(\mathrm{~b}_{1}\right)$ are the in-plane and out-of-plane $\mathrm{C}_{3}$-bending vibrations and $\nu_{3}\left(\mathrm{a}_{1}\right)$ and $\nu_{6}\left(\mathrm{~b}_{2}\right)$ are the vdW stretching and bending vibrations.

Of all the $\mathrm{C}_{3}-\mathrm{Kr}$ emission spectra, those from the vdW levels of the $\tilde{A}, b^{2-}$ state (b refers to the bending of the $C_{3}$ portion of the complex) shown in Fig. 3 are the simplest, with almost no activity in the ground state vdW modes. In this figure both even and odd quanta of the $\mathrm{C}_{3}$-bending vibration can be seen, suggesting that both the upper and lower states of the Kr complex are nonlinear. A Franck-Condon node occurs at the expected position of the $\tilde{X}, v_{2}{ }^{\prime \prime}+v_{4}{ }^{\prime \prime}=2$ levels (near $\nu_{\text {laser }}-140 \mathrm{~cm}^{-1}$ ). A similar Franck-Condon pattern is found in the Ar complex, ${ }^{10}$ though the latter has fewer levels with $v_{\mathrm{b}}{ }^{\prime \prime}=$ odd. In contrast, it is interesting to note that the $v_{2}{ }^{\prime \prime}$ $+v_{4}{ }^{\prime \prime}=2$ levels are observed in the Ne complex. ${ }^{18}$

Following the same procedure as described in Sec. VI of Ref. 10, the PHO model has been used to fit the observed $\mathrm{C}_{3}$-bending vibrational levels of the ground electronic state of the Kr complex. A satisfactory fit could be obtained if the
TABLE II. The energies and vibrational assignments of the lower levels observed from the emission of seventeen $\mathrm{C}_{3}-\mathrm{Kr}$ upper levels at $25016.6,{ }^{\text {a }} 25017.1,25020.6,{ }^{\text {b }}$ 25031.8, ${ }^{\mathrm{c}} 25045.4,{ }^{\text {d }} 25507.9,25511.1,25513.0$, $25420.6,^{\mathrm{e}} 25424 .,^{\mathrm{f}} 25446.6,{ }^{\mathrm{g}} 25734.5,{ }^{\mathrm{h}} 25736.1,{ }^{\mathrm{i}} 25737.0,25738.0,{ }^{\mathrm{j}} 25749.7,{ }^{\mathrm{k}}$ and $25768.4 \mathrm{~cm}^{-1}$.

| Vibrational assignment ${ }^{1}$ | $v_{\mathrm{b}}{ }^{\prime}=2^{-}$ |  |  |  |  | $v_{\mathrm{b}}{ }^{\prime}=2^{+}$ |  |  | $v_{\mathrm{b}}{ }^{\prime}=4^{-}$ |  |  | $v_{1}{ }^{\prime}=1$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 25016.6 | 25017.2 | 25020.6 | 25031.8 | 25045.4 | 25507.9 | 25511.1 | 25513.0 | 25420.6 | 25424.3 | 25446.6 | 25734.5 | 25736.1 | 25737.0 | 25738.0 | 25749.7 | 25768.4 |
| $\mathrm{b}_{0}$ |  |  |  |  |  |  |  |  |  |  |  | 0.0 | 0.0 |  |  |  |  |
| $\mathrm{b}_{0} 3_{1}$ |  |  |  |  |  | 36.7 |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{b}_{0} 3_{1} 6_{2}$ | 50 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{b}_{1}$ |  |  |  |  |  |  |  | 63 |  |  |  |  |  |  |  |  |  |
| $\mathrm{b}_{1} 6_{3}$ |  |  |  |  |  |  |  |  |  |  |  | 89 | 87.3 |  |  |  |  |
| $2_{1} 6_{1}$ |  |  |  | 122 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $2{ }_{1} 6_{3}$ |  |  |  |  | 135 |  |  |  |  |  | 138 |  |  |  |  |  |  |
| ? |  |  |  |  |  |  |  |  |  | 141 |  |  |  |  |  |  |  |
| $2_{1} 4_{2} 6_{1}$ |  |  |  |  |  |  |  |  |  |  |  |  |  | 209 | 210 |  |  |
| $22_{2}{ }_{1}$ |  |  |  |  |  |  |  |  |  |  |  | 219 | 219.2 |  |  | 218.4 |  |
| $22_{1} 6_{1}$ | 229 | 225.5 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 230 |
| $2_{2} 4_{1} 6_{3}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 246 |
| $22_{2} 3_{1} 4_{1}$ |  |  |  |  |  |  |  |  | 253.2 | 256.2 |  |  |  |  |  |  | 251(b) ${ }^{\text {m }}$ |
| $2{ }_{1} 4_{3}$ | 268 | 265.6 | 273 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $2_{1} 4_{3} 6_{1}$ |  |  |  | 281 |  |  |  |  |  |  | 279 |  |  |  |  |  |  |
| $2_{1} 4_{3} 62$ |  |  |  |  |  | 289 |  | 288 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | 293 |  | 293 |  |  |  |  | 294 |  |  | 292 |  |  |
| $22_{2}$ | 296.4 |  |  |  |  |  |  |  |  |  |  |  |  | 298 |  |  |  |
| $2_{1} 3_{1} 4_{3}$ |  |  |  |  |  |  |  |  |  |  |  |  | 302.9 |  |  | 305.3 |  |
| $22_{2} 6_{2}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 313 |
| $2{ }_{1} 4_{4}$ | 334 | 333.6 | 336 |  |  |  |  |  | 330 | 332 |  |  |  |  |  |  |  |
|  |  |  |  |  |  | 340.5 | 344 |  | 340 |  |  |  |  | 340 | 338 |  |  |
| $2_{1} 4_{4} 62$ |  | 348.4 | 347 |  |  |  |  | 347 |  |  |  |  |  |  |  | 349.5 |  |
| $2_{1} 4_{4} 6_{3}$ |  |  |  | 354.7 |  |  |  |  |  |  | 356 |  |  |  |  |  |  |
| $22_{3}$ | 360 | 358.4 |  |  |  |  |  | 359 |  |  |  |  |  |  |  |  |  |
|  |  |  | 363 | 363 |  |  |  |  |  |  |  |  |  |  |  |  | 364 |
| $2{ }_{1} 3_{1} 4_{4}$ |  |  |  |  | 370 |  |  |  |  |  |  | 369 | 370.4 |  |  |  |  |
|  |  |  |  | 375 |  |  |  |  | 373.6 |  |  |  |  |  |  |  |  |
| $23_{1} 4_{4} 6_{1}$ |  |  |  |  |  |  |  | 378 |  | 378 |  |  |  |  |  | 380 |  |
| $23_{31}$ |  |  |  |  | 387 |  |  |  | 392 |  |  |  |  | 390 | 388 |  |  |
| $\underline{23416}$ |  |  |  |  |  |  |  |  |  | 401 | 402 |  |  |  |  |  |  |

TABLE II. (Continued.)

| Vibrational assignment ${ }^{1}$ | $v_{\mathrm{b}}{ }^{\prime}=2^{-}$ |  |  |  |  | $v_{\mathrm{b}}{ }^{\prime}=2^{+}$ |  |  | $v_{\mathrm{b}}{ }^{\prime}=4^{-}$ |  |  | $v_{1}{ }^{\prime}=1$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 25016.6 | 25017.2 | 25020.6 | 25031.8 | 25045.4 | 25507.9 | 25511.1 | 25513.0 | 25420.6 | 25424.3 | 25446.6 | 25734.5 | 25736.1 | 25737.0 | 25738.0 | 25749.7 | 25768.4 |
| 2145 | 412 | 410.4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  | 416.5 |  |  | 417 | 416.7 | 418.5 |  |  |  |  |  |  |  |  |  |
| $2{ }_{1} 456$ |  |  |  | 426 |  |  |  |  |  |  |  |  |  | 427 | 427.9 |  |  |
|  |  |  |  |  |  | 431 |  |  |  |  |  |  |  |  |  |  |  |
| $2{ }_{1} 4_{5} 63$ |  |  |  |  |  |  | 434.6 |  |  |  |  |  | 435.1 |  |  |  |  |
| $22_{2} 4$ |  |  |  |  | 439 |  |  | 437.2 |  |  |  |  |  |  |  | 438.3 |  |
| $22_{2} 4_{4}{ }_{2}$ |  |  |  |  | 453 |  |  |  |  |  |  |  |  |  |  |  | 456 |
| $2_{2} 4_{4} 6_{3}$ |  |  |  |  |  | 464.1 | 462.6 | 461.8 |  |  |  |  |  |  |  |  |  |
| $2{ }_{1} 4_{6}$ | 470 | 469.1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 474.1 |  | 473 | 475 |  |  |  |  |  |  |  |
| $2_{1} 4_{6} 61$ |  | 481.3 | 477 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $2_{1} 4_{6} 6{ }_{2}$ |  |  | 490 | 486 |  |  |  |  | 487.7 |  |  |  |  |  |  |  |  |
| $22_{2}$ | 495 | 494.6 |  |  |  |  |  | 493 |  |  | 493 |  | 493.7 | 494.8 |  |  |  |
| $22_{5} 6_{1}$ |  |  |  |  | 501 |  |  |  |  |  | 500 |  |  |  | 498 |  |  |
| $2_{1} 3_{1} 4_{6}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 506.4 |  |
| $22_{2}{ }_{5}{ }_{2}$ |  |  |  |  |  |  |  |  | 511.7 |  |  |  |  |  |  |  |  |
| $22_{2}{ }_{5} 6$ |  |  |  |  |  |  |  | 519.0 |  | 517 | 517 |  |  |  |  |  | 519 |
| $22_{2} 4_{5}{ }_{4}$ |  |  |  |  |  |  |  |  | 526.8 |  |  | 526.3 |  | 527 |  |  |  |
| $22_{2} 4_{5}$ |  |  |  |  |  |  |  |  |  | 532 |  |  |  |  |  |  |  |
| $2{ }_{2}{ }_{1} 4_{5} 6_{1}$ |  |  |  |  |  |  |  |  | 541.3 |  | 540 | 538.4 | 540 |  |  |  |  |
| $22_{2} 4_{5} 6_{2}$ |  |  |  |  |  |  |  |  |  |  | 553 |  |  |  |  |  |  |
| $22_{2} 4_{5} 64$ |  |  |  |  |  | 564.2 | 562.1 |  | 560 | 563 |  |  |  |  |  |  |  |
| $2{ }_{1} 4_{7}$ | 573.5 | 574.7 |  |  |  |  |  | 572 |  |  | 569 | 573.4 | 575.1 |  |  |  |  |
|  |  |  | 579.2 |  |  |  | 578.1 |  |  |  |  |  |  |  |  |  |  |
| $2{ }_{1} 4_{7} 61$ |  |  |  |  |  |  |  |  |  |  |  | 582.5 |  |  |  |  |  |
| $2{ }_{1} 4_{7} 6_{2}$ |  |  |  | 589 |  |  |  |  |  |  | 587 |  |  |  |  | 586.0 | 588.7 |
| $2{ }_{1} 4_{7} 63$ |  |  |  |  |  | 596.4 |  |  |  |  |  |  |  |  |  |  |  |
| $2_{2} 4_{6}$ |  |  |  |  | 602.4 |  | 599.6 | 601.1 |  |  |  |  |  |  |  |  | 600 |
| $2_{1} 3_{1} 4_{7}$ |  |  |  |  |  | 611.2 | 612.4 |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | 616.4 |  | 616.2 |  |  |  |  |  |  |  |  |  |
| $2{ }_{2} 4_{6} 62$ |  |  |  |  |  |  | 622.7 |  |  |  |  |  |  |  |  |  |  |
| $2_{1} 4_{8}$ | 625.9 | 625.3 |  |  |  | 627.5 |  |  |  |  |  |  |  |  |  |  |  |
| $2_{1} 4_{8} 61$ |  |  | 633.5 |  |  |  |  | 634 | 636 |  |  |  |  |  |  |  |  |
|  |  |  |  | 637.3 |  |  | 637.3 |  |  | 639 |  |  |  |  |  |  |  |
|  | 647.2 | 645.6 |  |  |  | 649.6 |  |  |  |  |  |  |  |  |  |  |  |

TABLE II. (Continued.)

| Vibrational assignment ${ }^{1}$ | $v_{\mathrm{b}}{ }^{\prime}=2^{-}$ |  |  |  |  | $v_{\mathrm{b}}{ }^{\prime}=2^{+}$ |  |  | $v_{\mathrm{b}}{ }^{\prime}=4^{-}$ |  |  | $v_{1}{ }^{\prime}=1$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 25016.6 | 25017.2 | 25020.6 | 25031.8 | 25045.4 | 25507.9 | 25511.1 | 25513.0 | 25420.6 | 25424.3 | 25446.6 | 25734.5 | 25736.1 | 25737.0 | 25738.0 | 25749.7 | 25768.4 |
|  |  |  |  |  |  |  | 655 | 656 |  |  |  | 655.3 |  |  |  |  |  |
|  | 660.5 | 657.4 |  |  | 657.5 |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | 664 |  | 663.2 | 664 | 666 |  |  |
|  |  |  |  |  |  |  |  |  | 671 | 670 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | 676 |  |  |  |  | 677.1 |  |
|  |  |  |  |  |  |  |  |  |  |  | 694 |  |  | 694 | 694 |  | 692.5 |
|  |  |  |  |  |  |  |  |  | 701.2 | 704 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 706 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | 710.8 |  | 708.7 |  |
|  |  |  |  |  |  |  |  |  |  |  |  | 717.2 |  |  |  |  | 714 |
|  |  |  |  |  |  | 723 |  |  |  |  |  | 724.5 | 724.1 |  |  |  | 722 |
|  |  |  |  |  |  |  | 727.7 |  |  |  | 726.7 |  |  |  |  | 726.7 |  |
|  |  |  |  |  |  | 733.5 |  | 732.0 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 740.4 | 743 |  |  |  |  |  |  |  |
| $2{ }_{1} 49$ | 755.5 | 752.3 |  |  |  | 757.7 |  |  |  |  |  |  |  | 757 | 756 |  |  |
|  |  |  | 760 |  |  |  | 759 | 761.9 |  |  |  |  |  |  |  |  |  |
| $2{ }_{1} 4_{9} 61$ |  |  |  |  |  |  |  |  |  |  | 766 |  |  |  |  | 766 |  |
| $2{ }_{1} 4_{9} 62$ |  |  |  | 772 |  | 774.5 |  |  |  |  |  |  |  |  |  |  |  |
| $21_{19} 6_{3}$ |  |  |  |  |  |  | 780.6 | 780.2 |  |  |  |  |  |  |  |  |  |
| $22_{8}$ | 785.2 |  |  |  | 783 |  |  |  |  |  |  |  |  | 785 | 785 |  | 783 |
| $23_{1} 3_{1} 9$ |  |  |  |  |  |  |  | 789 |  |  |  |  | 787.5 |  |  |  |  |
| $22_{8} 6_{1}$ |  |  |  |  |  |  |  | 793 |  |  |  |  |  |  |  |  |  |
| $2{ }_{1} 3_{1} 4_{9} 6_{1}$ |  |  |  |  |  |  | 798.9 |  |  |  |  |  |  |  |  | 797 |  |
| $24_{1}{ }_{10}$ | 799.6 | 799.6 | 802 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | 805.3 |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 819.5 |  |  |  |  |  |  | 817.6 |  |  |  |  |  |  |  |  |
|  | 822.3 |  |  |  |  |  |  |  |  |  |  |  |  |  | 824 |  | 820 |
|  |  |  |  |  |  | 833.2 |  |  |  |  |  |  |  |  |  |  |  |
| $23_{1} 4_{10}$ |  |  |  |  | 837 |  | 836.8 | 836.3 | 838 | 839 | 837 |  |  |  |  |  |  |
|  | 843.6 |  |  |  |  |  |  |  |  |  | 844.5 |  | 846 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | 852.1 | 850 |  | 849 | 852 |  | 852 |
|  |  |  | 857 |  |  | 858.5 | 859.4 | 856.5 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  | 862.1 | 861.5 |  |  |  |  | 862 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | 874 |  |  | 878 |
|  | 886 |  |  |  |  |  |  |  | 887 | 887 | 884.3 |  |  |  |  | 886 |  |

TABLE II. (Continued.)

|  | $v_{\mathrm{b}}{ }^{\prime}=2^{-}$ |  |  |  |  | $v_{\mathrm{b}}{ }^{\prime}=2^{+}$ |  |  | $v_{\mathrm{b}^{\prime}}=4^{-}$ |  |  | $v_{1}{ }^{\prime}=1$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Vibrational assignment ${ }^{1}$ | 25016.6 | 25017.2 | 25020.6 | 25031.8 | 25045.4 | 25507.9 | 25511.1 | 25513.0 | 25420.6 | 25424.3 | 25446.6 | 25734.5 | 25736.1 | 25737.0 | 25738.0 | 25749.7 | 25768.4 |
|  |  |  |  |  |  |  |  | 890.6 | 894 | 893 |  |  |  |  |  |  | 895 |
|  |  |  |  |  |  | 907.9 |  |  |  |  |  |  |  |  |  |  | 902 |
|  |  |  |  |  |  |  | 913.2 | 912.6 |  |  | 911.7 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  | 922.6 |  |  |  |  |
|  |  |  |  |  |  | 930.1 |  |  | 934 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 939 |  |  | 939 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 945.1 |  |  |  |  | 943.1 | 944 | 945 |  |  |
|  |  |  | 958 |  |  |  | 959.9 |  |  |  |  |  |  |  |  | 955 |  |
|  |  |  |  |  |  | 970.7 |  |  |  |  |  |  |  |  |  |  | 971 |
|  |  |  |  |  |  |  | 975 | 975.6 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 983 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 1016.5 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 1032.8 |

[^0]TABLE III. The observed and calculated $\mathrm{C}_{3}$-bending vibrational levels of $\mathrm{C}_{3}-\mathrm{Kr}$ using the PHO model. All parameters and the standard deviation of the fit are in units of $\mathrm{cm}^{-1}$.

| $v_{\mathrm{b}}$ | $\left(v_{2}, v_{4}\right)$ | obs | obs-cal |
| :---: | :---: | :---: | :---: |
| 4 | $(1,3)$ | 268.0 | 7.1 |
|  | $(2,2)$ | 296.4 | 9.7 |
| 5 | $(1,4)$ | 334.0 | 1.7 |
|  | $(2,3)$ | 360.0 | 1.5 |
| 6 | $(1,5)$ | 412.0 | 4.0 |
|  | $(2,4)$ | 438.0 | 3.2 |
| 7 | $(1,6)$ | 470.0 | -17.8 |
|  | $(2,5)$ | 495.0 | $-20.2$ |
| 8 | $(1,7)$ | 574.0 | 2.6 |
|  | $(2,6)$ | 600.0 | 0.4 |
| 9 | $(1,8)$ | 626.0 | - |
| 10 | $(1,9)$ | 756.0 | 6.6 |
|  | $(2,8)$ | 785.0 | 5.9 |
|  | $\sigma^{\text {a }}$ | 9.1 |  |
|  | $\mathrm{V}_{1}$ | 0.0(fixed) |  |
|  | $\left\|V_{2}\right\|$ | $6.3 \pm 0.3$ |  |
| $\begin{aligned} & v_{2}=111.2(72), \\ & x_{44}=3.07(42), \end{aligned}$ | $\begin{gathered} v_{4}=40.2(33), \\ \sigma=7.1 \mathrm{~cm}^{-1} \end{gathered}$ | $x_{22}=-10.0(\text { fixed }),$ | $x_{24}=5.0(15)$, |

${ }^{a}$ One standard deviation of the error of the fit.
observed levels of each $v_{\mathrm{b}}{ }^{\prime \prime}$ manifold were assigned as $\left(v_{2}{ }^{\prime \prime}\right.$ $\left.=1, v_{4}{ }^{\prime \prime}=v_{\mathrm{b}}{ }^{\prime \prime}-1\right)$ and ( $v_{2}{ }^{\prime \prime}=2, v_{4}{ }^{\prime \prime}=v_{\mathrm{b}}{ }^{\prime \prime}-2$ ). The results are listed in Table III. The observed $\mathrm{C}_{3}$-bending vibrational levels with $v_{\mathrm{b}}{ }^{\prime \prime}=9$ have not been included in the fit because they give residuals of more than three standard deviations of the fit. (This was the case also with the Ar complex.) The poor fit for the $v_{\mathrm{b}}{ }^{\prime \prime}=9$ level in both the complexes possibly results from the lack of precise measurements for the odd $v_{\mathrm{b}}{ }^{\prime \prime}$ levels $(\geq 11)$ of free $\mathrm{C}_{3},{ }^{15,19,20}$ which are the basis states in the PHO model.

The dipole-induced dipole interaction strength of the Kr complex obtained from this fit is $\left|\mathrm{V}_{2}\right|=6.3(3) \mathrm{cm}^{-1}$, which is about 1.3 times that of the Ar complex, ${ }^{10}$ where $\left|\mathrm{V}_{2}\right|$ $=4.8(4) \mathrm{cm}^{-1}$. The increase in $\left|\mathrm{V}_{2}\right|$ can be explained by the larger polarizability of Kr compared to Ar. Given the polarizabilities of the Kr and Ar atoms $\left(2.484 \times 10^{-24}\right.$ and 1.641 $\times 10^{-24} \mathrm{~cm}^{3}$, respectively) ${ }^{21}$ and the ab initio calculated bond length of $\mathrm{C}_{3}-\mathrm{Ar}(3.9 \AA),{ }^{10}$ the values of $\mathrm{V}_{2}$ allow the bond length of the $\mathrm{C}_{3}-\mathrm{Kr}$ complex to be estimated as 4.0 $\AA$, using the formula for dipole-induced dipole interaction. ${ }^{22}$ The fairly small change in the vdW bond length from the Ar complex to the Kr complex, which is consistent with previous reports on CO and $\mathrm{NO},{ }^{1,2}$ is supported by our $a b$ initio calculations. Calculations ${ }^{23}$ of the Kr complex could only be made with smaller basis sets [aug-cc-pVTZ (C) (Refs. 24 and 25) and aug-cc-pVTZ-pp (Kr) (Ref. 26)] than those used for the Ar complex (cc-pVQZ). It is expected that the vdW bond length predicted by the aug-cc-pVTZ basis set will be shorter by $0.1 \AA$ than that predicted by ccpVQZ . The $a b$ initio calculated vdW bond length of the Kr complex is $3.9 \AA$. Applying the same corrections for the different basis sets as those used for the $\mathrm{C}_{3}-\mathrm{Ar}$ complex, the bond length changes to $4.0 \AA$, which (possibly coinciden-
tally) is the same as that given by the dipole-induced dipole model.

The $\mathrm{C}_{3}$-bending levels have also been fitted with a two-dimensional anharmonic oscillator model, giving $\nu_{2}=111.2(72)$ and $\nu_{4}=40.2(33) \mathrm{cm}^{-1}$ (see Table III). The large anharmonicities obtained from the fit result from the large-small staggering of the level spacings of the $\nu_{4}$ mode, which possibly indicate that the vdW motion has a double minimum vibrational potential. Unfortunately, the PHO model does not take into account the coupling of $\nu_{4}$ with the vdW bend and vdW stretch. From Table II, three other vibrational intervals, 27(2), 37(2), and 8(2) $\mathrm{cm}^{-1}$, can be identified. The $27(2) \mathrm{cm}^{-1}$ interval is assigned as the separation of different components of a $v_{\mathrm{b}}$-polyad, such as ( $v_{2}=1$, $v_{4}=v_{\mathrm{b}}-1$ ) and ( $v_{2}=2, v_{4}=v_{\mathrm{b}}-2$ ), where $v_{2}+v_{4}$ $=v_{\mathrm{b}}$. The $37(2)$ and $8(2) \mathrm{cm}^{-1}$ intervals are assigned to the $\nu_{3}$ and $\nu_{6}$ vibrations of the Kr complex, respectively. It is possible to estimate the vdW stretching frequency, $\nu_{3}$, by solving a one-dimensional Schrödinger equation using a perturbation method; the vdW stretching potential was first obtained from $a b$ initio calculations ${ }^{23}$ at the level of $\operatorname{CCSD}(\mathrm{T}) /$ aug-cc-pVTZ $(\mathrm{C})$ and aug-cc-pVTZ-pp ( Kr ), and the data were then fitted to a Morse-like function,

$$
\begin{equation*}
V(R)=V_{0}+a \exp (-b R)+c \exp (-d R) \tag{1}
\end{equation*}
$$

Taking $\rho(\angle \mathrm{C}-\mathrm{C}-\mathrm{C})=170^{\circ}$ and $\phi$ (the in-plane angle, at the center of mass of the $\mathrm{C}_{3}$ molecule, between its $a$-axis and the Xe atom) $=90^{\circ}$, the $\nu_{3}$ frequency is given as $38.6 \mathrm{~cm}^{-1}$ and the anharmonicity constant $x_{33}$ as $-1.355 \mathrm{~cm}^{-1}$. A small frequency interval of $3-5$ $\mathrm{cm}^{-1}$, found in the emission spectra, could not be assigned. As a result, some of the levels, particularly those with $v_{\mathrm{b}}{ }^{\prime \prime}=9$, have not been assigned in Table II.

## V. WAVELENGTH-RESOLVED EMISSION SPECTRA OF THE $\mathrm{C}_{3}-\mathrm{Xe}$ COMPLEX

As is the case with the other $\mathrm{C}_{3}-\mathrm{Rg}$ vdW molecules, no $\underset{\sim}{\mathrm{X}}$-complex features were observed near the $(0,0)$ band of the $\tilde{\mathrm{A}}-\tilde{\mathrm{X}}$ system of $\mathrm{C}_{3}$. Table IV lists the ground state energy levels given by the wavelength-resolved emission spectra from seven $\mathrm{C}_{3}-\mathrm{Xe}$ bands near the $2^{2-}{ }_{0}, 2^{2+}{ }_{0}$, and $2^{4-}{ }_{0}$ bands of $\mathrm{C}_{3}$. Representative spectra are illustrated in Figs. 6 and 7. Because the fluorescence intensity from the Xe -complex is quite weak, the slit width of the monochromator had to be widened to $100 \mu \mathrm{~m}$ in order to record emission spectra from bands B and C in Fig. 6; the spectral resolution of the emission from these two bands is therefore reduced to about $20 \mathrm{~cm}^{-1}$. Band A in Fig. 6 and bands D and E in Fig. 7 are stronger, so that their emission spectra could be recorded with slightly better resolution, $12 \mathrm{~cm}^{-1}$. As Fig. 7 shows, the emission features with displacements, $\nu_{\text {laser }}-v=600-1000 \mathrm{~cm}^{-1}$ show signs of diffuseness. It is not clear whether this is caused by predissociation or spectral congestion. However the emission spectra contain no bands that can be assigned to $\mathrm{C}_{3}$ itself, suggesting that electronically excited $\mathrm{C}_{3}$ is not formed when these bands of the complex are excited. (This is the case also in the emission spectra of the Ar and Kr complexes. ${ }^{10}$ ) We


FIG. 6. Top figure: excitation spectrum of the Xe complex near the $2^{2-}{ }_{0}$ band of free $\mathrm{C}_{3}$. Below are traces of the wavelength resolved emission spectra obtained by exciting the blended $R(0)$ and $Q(2)$ lines of $C_{3}$ and by exciting the Xe complex at the vdW bands labeled A-C, respectively.
therefore prefer to attribute the diffuseness to spectral congestion.

Figure 6 shows that the emission spectra from the $\mathrm{C}_{3}-$ Xe bands near the $2^{2-}{ }_{0}$ band of $\mathrm{C}_{3}$ are surprisingly simple: only even quanta of the $\mathrm{C}_{3}$-bending vibration were observed. These spectra resemble that of free $\mathrm{C}_{3}$, barring a FranckCondon node at the second member of the progression, and suggest that the observed level structure of the ground-state complex is that of a linear molecule. The observed progression can thus be assigned as $v_{4}{ }^{\prime \prime}=2 n, n=2-5$, where $\nu_{4}(\pi)$ is the $\mathrm{C}_{3}$ bending vibration. It is found that the levels of $v_{4}{ }^{\prime \prime}=2,4$, and 6 are shifted to higher frequency compared to those of free $\mathrm{C}_{3}$, in contrast to what is found in the Ar and Kr -complexes. This implies that the Xe atom bonds more weakly to $\mathrm{C}_{3}$ in its bending-excited levels than to $\mathrm{C}_{3}$ in its zero-point level; the binding strengths of the $v_{4}{ }^{\prime \prime} \geq 2$ levels increase progressively as $v_{4}{ }^{\prime \prime}$ increases, and eventually those of $v_{4}{ }^{\prime \prime} \geq 8$ become larger than that of $v_{4}{ }^{\prime \prime}=0$.

The observed $\mathrm{C}_{3}$-bending vibrational levels of the $\mathrm{C}_{3}$ $\mathrm{Ar},{ }^{10} \mathrm{C}_{3}-\mathrm{Kr}$, and $\mathrm{C}_{3}-\mathrm{Xe}$ complexes are plotted in Fig. 8 along with those of free $\mathrm{C}_{3} .{ }^{15,27}$ The Ar- and Kr-complexes both show the same trends: as the bending quantum number increases, the $\mathrm{C}_{3}$-bending frequencies (level spacings) of these two complexes are progressively red-shifted relative to those of free $\mathrm{C}_{3}$. The magnitude of the red-shift is roughly proportional to the polarizabilities of the Ar and Kr atoms, as


FIG. 7. Top trace: Excitation spectrum of $\mathrm{C}_{3} \mathrm{Xe}$ (bands D and E) and $\mathrm{C}_{3}$ (labeled $\mathrm{R}(0)+\mathrm{Q}(2)$ ) near the $2^{2+}{ }_{0}$ band of free $\mathrm{C}_{3}$. Wavelength-resolved emission spectra shown in the lower traces were obtained by exciting $C_{3}$ and the Xe complex at the labeled frequencies, respectively.
discussed in Sec. IV. The level structure of the Xe complex is not easily understood. The first few levels are shifted to higher energy than those than free $\mathrm{C}_{3}$; above $v_{4}{ }^{\prime \prime}=4$ the energy level spacing becomes more regular, reaching a value of about $169 \mathrm{~cm}^{-1}\left(2 v_{4}\right)$. More discussion of the vibrational


FIG. 8. The $\mathrm{C}_{3}$-bending levels of free $\mathrm{C}_{3}, \mathrm{C}_{3}-\mathrm{Ar}, \mathrm{C}_{3}-\mathrm{Kr}$, and $\mathrm{C}_{3}-\mathrm{Xe}$.

TABLE IV. The energies and vibrational assignments of the lower levels observed from the emission from seven $\mathrm{C}_{3}-$ Xe upper levels at 25004.7 , ${ }^{\mathrm{a}} 25015$, ${ }^{\mathrm{b}}$ $25026.6,{ }^{\mathrm{c}} 25406.6,25430.9,25494.1,^{\mathrm{d}}$ and $25516.7^{\mathrm{e}} \mathrm{cm}^{-1}$.

| Vibrational assignment ${ }^{\text {f }}$ | $v_{4}^{\prime}=2^{-}$ |  |  | $v_{4}^{\prime}=4^{-}$ |  | $v_{4}^{\prime}=2^{+}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 25004.7 | 25015 | 25026.6 | 25406.6 | 25430.9 | 25494.1 | 25516.7 |
| $\mathrm{b}_{2}$ |  |  |  |  | 127 |  | 128 |
| $\mathrm{b}_{2} 3_{1}$ (or $4_{2}$ ) | 168 |  |  |  | 172 |  |  |
| $\mathrm{b}_{2} 3_{1} 5_{2}\left(\right.$ or $4_{2} 5_{2}$ ) |  |  |  |  |  | 188(vw) ${ }^{\text {g }}$ |  |
| $\mathrm{b}_{2} 3_{1} 5_{3}\left(\right.$ or $4_{2} 5_{3}$ ) |  |  |  |  | 200(w) ${ }^{\text {g }}$ |  |  |
| $\mathrm{b}_{4}$ ? | 254 |  | 257(w) |  |  |  |  |
| $\mathrm{b}_{4} 5_{2}$ ? |  |  |  |  |  |  | 278 |
| ? |  |  |  |  | 283(vw) |  |  |
| $\mathrm{b}_{4} 3_{1}$ ? |  |  |  |  |  |  | 294(sh) ${ }^{\text {g }}$ |
| $\mathrm{b}_{4} 3_{1} 5_{2}$ ? |  |  |  | 316 | 312 |  |  |
| 44 | 329 |  |  |  |  | 328(vw) |  |
| $45_{1}$ | 340(sh) | 340 |  |  | 337 |  |  |
| $445_{2}$ |  |  | 349 |  | 347 |  |  |
| 4453 |  |  |  |  |  |  | 354 |
| $4_{4} 5_{4}$ |  |  | 366 | 363 |  |  |  |
| $43_{1}$ |  |  |  | 370(sh) |  |  |  |
| $4_{4} 3_{1} 5_{1}$ |  |  |  | 377(sh) |  | 374 |  |
| $43_{1} 5_{2}$ |  |  |  |  | 384(b) |  |  |
| 45 |  |  |  |  | 393(b) |  | 396 |
| $4_{5} 5_{2}$ |  |  |  |  | 409(vw) | 406 |  |
| $4_{5} 5_{4}$ |  |  |  |  | 426(w) |  | 426 |
| $4_{5} 5_{6}$ |  |  |  |  |  |  | 443 |
| $45_{5}$ |  |  |  |  | 448 | 451 |  |
| $4_{6}$ | 462 |  |  | 460 |  | 463(sh) | 465(sh) |
| $4{ }_{6} 5_{1}$ | 475 | 473 |  |  |  |  | 473 |
| $4{ }_{6} 5_{2}$ |  |  | 481 |  |  |  |  |
| $4_{6} 5_{3}$ |  |  |  |  | 489 | 486 | 491 |
| $4_{6} 3_{1}$ |  |  | 504 | 505 |  |  |  |
| $4_{6} 3_{1} 5_{1}$ |  |  |  | 515 |  |  | 511 |
| $4_{6} 3{ }_{1} 5_{3}$ |  |  |  |  | $529(\mathrm{~b})^{\mathrm{g}}$ |  |  |
| 47 |  |  |  | 537 | 539(b) | 542(sh) |  |
| $4_{7} 5_{1}$ |  |  |  | 548(sh) |  | 552 |  |
| $475_{2}$ |  |  |  | 555(sh) | 559(b) |  |  |
| $4_{7} 5_{3}$ |  |  |  |  | 572(sh) |  | 567 |
| $4_{7} 3_{1}$ |  |  |  |  |  |  | 575 |
| $4_{7} 3_{1} 5_{2}$ |  |  |  |  |  | 592(b) |  |
| $4_{7} 3_{1} 5_{4}$ |  |  |  |  |  | 605(b) |  |
| $4_{7} 3_{2}$ |  |  |  |  |  |  | 611 |
| 48 | 616 |  |  |  |  | 614(b) |  |
| $4{ }_{8} 5_{1}$ | 624(sh) |  |  | 625 |  | 623 | 627 |
| $4_{8} 5_{1}$ ? |  | 630 |  |  | 631 |  | 635(sh) |
| $4_{8} 5_{2}$ |  |  | 639 |  |  |  | 642(sh) |
| 4853 |  |  |  |  | 648 |  | 650(sh) |
| $4_{8} 3_{1}$ |  |  |  | 659 |  |  | 657(sh) |
| $4_{8} 3_{1} 5_{2}$ |  |  |  | 680 | 683 |  |  |
| $4{ }_{8} 3_{1} 5_{3}$ |  |  |  |  | 695(sh) |  |  |
| 49 |  |  |  |  | 703(sh) |  |  |
| 4951 |  |  |  | 709 | 710(sh) | 713 |  |
| 4952 |  |  |  | 724 |  |  |  |
| 4953 |  |  |  | 734 |  |  | 729(b) |
| 4954 |  |  |  |  |  |  | 740(b) |
| 4931 |  |  |  | 746(sh) | 747(sh) | 747 |  |
| $4{ }_{9} 3_{1} 5_{1}$ |  |  |  | 760(sh) | 758 |  |  |
| $\underline{49315}$ |  |  |  |  | 771(sh) | 772 | 768(b) |

TABLE IV. (Continued.)

| Vibrational assignment ${ }^{\mathrm{f}}$ | $v_{4}^{\prime}=2^{-}$ |  |  | $v_{4}^{\prime}=4^{-}$ |  | $v_{4}^{\prime}=2^{+}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 25004.7 | 25015 | 25026.6 | 25406.6 | 25430.9 | 25494.1 | 25516.7 |
| $4_{9} 3{ }_{1} 5_{3}$ |  |  |  | 778 |  |  |  |
| $4_{10}$ | 785 |  |  |  |  |  | 790(b) |
| $4_{10} 5_{1}$ |  |  |  |  |  |  | 798(sh) |
| $4_{10} 5_{2}$ |  | 803 |  | 805 |  |  |  |
| $4_{10} 5_{3}$ |  |  | 810 |  |  |  |  |
| $4_{10} 5_{4}$ |  |  |  |  |  | 823 |  |
| $4_{10} 3_{1}$ |  |  |  | 829 | 828 |  | 828(sh) |
| $4_{10} 3_{1} 5_{1}$ |  |  |  |  |  |  | 836(b) |
| $4_{10} 3_{1} 5_{2}$ |  |  |  | 845 |  |  | 844(b) |
| $4_{10} 3_{1} 5_{3}$ |  |  |  |  | 850 |  |  |
| $4_{10} 3_{1} 5_{4}$ |  |  |  |  |  |  | 856(sh) |
| $4_{10} 3_{1} 5_{5}$ |  |  |  |  |  |  | 861(sh) |
| $4_{11}$ |  |  |  | 866 | 867 |  |  |
| $4_{11} 5_{2}$ |  |  |  | 881 |  |  |  |
| $4_{11} 5_{3}$ |  |  |  |  | 893 | 895 |  |
| $4_{11} 5_{4}$ |  |  |  | 899 |  |  |  |
| $4_{11} 3_{1}$ |  |  |  |  | 909(sh) |  | 911(sh) |
| $4_{11} 3_{1} 5_{1}$ |  |  |  |  |  | 915 | 918 |
| $4_{11} 3_{1} 5_{3}$ |  |  |  |  |  | 933 |  |
| $4_{11} 3_{1} 5_{4}$ |  |  |  |  |  |  | 938 |
| $4_{12}$ |  |  |  |  |  | 954 | 951 |
| $4_{12} 5_{2}$ |  |  |  |  |  |  | 975(b) |
| $4_{12} 5_{3}$ |  |  |  |  |  |  | 981(b) |

${ }^{\text {a }}$ Band A of Fig. 6 .
${ }^{\mathrm{b}}$ Band B of Fig. 6.
${ }^{\text {c }}$ Band C of Fig. 6.
${ }^{\mathrm{d}}$ Band D of Fig. 7.
${ }^{\mathrm{e}}$ Band E of Fig. 7.
${ }^{\mathrm{f}} \nu_{3}$ : vdW stretch frequency, $\nu_{4}: \mathrm{C}_{3}$-bending frequency, $\nu 5$ : vdW bending frequency.
$\mathrm{g}_{\mathrm{Vw}}$; very weak; w: weak; sh: shoulder of a broad feature; b: broad.
frequencies and the geometries of the Xe -complex is given in Secs. VI B and VII.

## VI. AB INITIO CALCULATIONS OF THE C $\mathrm{C}_{3}-\mathrm{Xe}$ COMPLEX

## A. Geometry and energy calculations

$A b$ initio calculations of its ground state potential surface have been carried out for the $\mathrm{C}_{3}-\mathrm{Xe}$ complex. An effective core potential was chosen to describe the inner $1 s$ - $3 d$ electrons of the Xe atom..$^{26}$ The carbon atoms and the outer 26 electrons of the Xe atom were treated with aug-cc-pVTZ basis sets. ${ }^{24-26}$ No attempt was made to use larger basis sets, such as pVQZ, because these do not run efficiently on our computer system ( 64 bits, 32 Gigabytes memory).

The global minimum of the potential surface is found to be a planar slightly distorted Y-shaped complex, (Y), where the structure is $\rho\left(\mathrm{C}_{3}\right.$ bond angle $)=170^{\circ}, \mathrm{r}(\mathrm{C}-\mathrm{C}$ bond length $)$ $=1.298 \AA$, and $\mathrm{R}(\mathrm{vdW}$ bond length, Xe to the center of mass of $\mathrm{C}_{3}$ ) $=4.0 \AA$. There are two equivalent minima, which correspond to the in-plane bending angles $\phi=240^{\circ}$ and $300^{\circ}$. (The symmetrical Y-shaped configuration is defined as $\phi=270^{\circ}$, so that the Xe atom lies slightly off the "stalk" of the Y.) Another isomer where the $\mathrm{C}_{3}$ molecule is bent in the
opposite direction $(\uparrow)$ lies about $20 \mathrm{~cm}^{-1}$ higher. We call this T-shaped, from the direction of the serifs on the printed letter T. (This isomer is defined as having $\phi<180^{\circ}$, while the Y-shaped isomer has $\phi>180^{\circ}$.) These two isomers will interconvert rapidly, as the $\mathrm{C}_{3}$ molecule executes its zero-point bending motion.

Isomerization by internal rotation about the inertial $c$-axis, which is perpendicular to the plane of the Xe complex, is less likely because the minimum energy pathway requires that a barrier of about $150 \mathrm{~cm}^{-1}$ be surmounted. A saddle point is found at $\phi=175^{\circ} \pm 20^{\circ}$ or $5^{\circ}$ $\pm 20^{\circ}, \mathrm{R}=5.2-5.4 \AA$. It corresponds to another isomer which we call the L-isomer, where the Xe atom lies close to one of the terminal carbon atoms along the inertial $a$ axis of $\mathrm{C}_{3}$. This isomer lies about $120 \mathrm{~cm}^{-1}$ above the Y-isomer.

We have examined the shape of the potential surface at values of $\rho$ corresponding to the classical turning points of the bending vibration of free $\mathrm{C}_{3}$ for $v=0,2,4$, and 6 . From the bending potential curve of Ref. 19, these turning points occur near $\rho=142^{\circ}, 125^{\circ}, 118^{\circ}$, and $112^{\circ}$, respectively. When the $\mathrm{C}_{3}$ molecule is bent, up to about $\rho=120^{\circ}$, no saddle point is found near $\phi \sim 0^{\circ}$ or $180^{\circ}$. However, when $\rho$ is $118^{\circ}$, an L-isomer of nearly linear shape ( $\wedge-$ ), a local minimum, can be identified near $\phi=180^{\circ}-205^{\circ}$ or $335^{\circ}-360^{\circ}$, with


FIG. 9. Contour plot of the $\operatorname{CCSD}(\mathrm{T})$ energies of the $\mathrm{C}_{3}-\mathrm{Xe}$ vdW complex versus the $(x, y)$ coordinates of the Xe atom relative to the center-of-mass of bent $C_{3}$ (at $\rho=112^{\circ}$ and $r(C-C)=1.298 \AA$ ). The energies are expressed in units of $\mathrm{cm}^{-1}$ relative to the potential minimum of the complex. Contours with energies below $700 \mathrm{~cm}^{-1}$ are given for every $10 \mathrm{~cm}^{-1}$. Contours with energy above $700 \mathrm{~cm}^{-1}$ (shown only in the repulsive part) are given for every $100 \mathrm{~cm}^{-1}$.
$\mathrm{R}=4.8-5.0$ A. If $\rho$ decreases further, the Xe atom bonds even more strongly along the $a$-axis of the bent $\mathrm{C}_{3}$ molecule; at $\rho=112^{\circ}$, the structure corresponds to $\phi$ $=0^{\circ}$ or $180^{\circ}$ and $\mathrm{R}=4.8 \AA$ \& the energy of the L-isomer is then $\sim 60 \mathrm{~cm}^{-1}$ below that of the Y-isomer for the same $\mathrm{C}_{3}$-bending excitation. Cuts through the potential surface of the Xe-complex at $\rho=112^{\circ}$ are illustrated in Figs. 9-11.

Figure 9 is a contour plot of the $\operatorname{CCSD}(\mathrm{T})$ energies of the Xe complex at $\rho=112^{\circ}$ in the range $\mathrm{R}=3.6-5.4 \AA$. The instantaneous position of the Xe atom relative to the center-of-mass (C.M.) of the $\mathrm{C}_{3}$ molecule is expressed in Cartesian coordinates. The energies in Fig. 9 are relative to the global minimum of the ground electronic state of the Xe complex. The Y-shaped isomer is less stable than the T-shaped isomer at short vdW bond lengths, but this energy order reverses when $R$ is greater than $4.4 \AA$. At this point, the complex can undergo a fairly large amplitude vdW bending motion from Y-shape to near L-shape. If R is shorter than $4.8 \AA$, a fairly large barrier prevents the T-to- Y isomerization from occurring unless the $\mathrm{C}_{3}$ molecule bends out of plane. When R is greater than about $5 \AA$, there is essentially free internal rotation around the $c$-axis of the Xe-complex, which allows easy interconversion of the three isomers.

It is not easy to see the minima corresponding to the L-isomer in Fig. 9, because the grid of points is not fine enough. Figure 10 is an alternative representation of Fig. 9, showing how the two equivalent potential minima of the Yisomer move apart as the vdW bond length increases, giving rise to pronounced local minima near the L-configuration at
$\mathrm{R}=4.6-4.8 \AA$. They are marked with arrows in the figure. Large amplitude vdW bending motion would allow adiabatic Y-to-L conversion. Figure 11 shows a contour plot of the $\operatorname{CCSD}(\mathrm{T})$ energies at $\rho=112^{\circ}$ against the out-of-plane $\mathrm{C}_{3}$ bending angle, $\theta$, and the in-plane vdW bending angle, $\phi$, at a fixed vdW bond length, $\mathrm{R}=4.8 \AA$. It confirms that the complex prefers to be planar and that the L-isomer lies at a local minimum (i.e., $\phi \sim 0^{\circ}$ or $180^{\circ}$ ), representing a stable isomer when $\rho$ is small (i.e., for strongly bent $\mathrm{C}_{3}$, with large values of $v_{\text {bend }}$ ). In contrast, no L-isomer could be located in the potential of the $\mathrm{C}_{3}-\mathrm{Ar}$ complex.

Figure 9 also shows that, over the complete range $\rho=112-180^{\circ}$ which we have studied by ab initio calculation, the minimum energy pathway to dissociation is via the high vibrational levels of the L -isomer.

## B. Vibrational frequencies

Assuming that the rare gas atom perturbs the $\mathrm{C}_{3}$ bending motion only slightly, the $\mathrm{C}_{3}$-bending frequencies of the three possible isomers can be estimated from the $\operatorname{CCSD}(\mathrm{T})$ potential calculated at values of $\rho$ corresponding to the classical turning points (see Sec. IVA). The value of R was taken as $3.8 \AA$. It has been shown that the potential curve of the $\mathrm{C}_{3}$ bending vibration of free $\mathrm{C}_{3}$ is very flat and that it requires a fairly large basis set to reproduce the observed vibrational levels. ${ }^{19,20}$ Using a small basis set such as aug-cc-pVTZ, a calculated frequency tends to be higher than the observed values. ${ }^{19,20}$ Our observed $\mathrm{C}_{3}$-bending intervals $\left[\mathrm{E}\left(v_{4}+2\right)\right.$


FIG. 10. The $\operatorname{CCSD}(\mathrm{T})$ energy curves of the $\mathrm{C}_{3}-\mathrm{Xe}$ vdW complex versus the in-plane vdW bending angle, $\phi$, for $\mathrm{R}=3.6-5.4 \AA$ at $\rho=112^{\circ}$ and $\mathrm{r}(\mathrm{C}-\mathrm{C})$
 $4.4 \AA,-\square-; 4.6 \AA,-\cdot \square-; 4.8 \AA,--; 5.0 \AA,-\square 5.2 \AA, \cdot \cdot \mathbf{\square} \cdot ; 5.4 \AA,--\Delta--$. Arrows indicate the minima corresponding to the L-isomer at $4.4,4.6$, and $4.8 \AA$.
$-\mathrm{E}\left(v_{4}\right)=133,155$, and $169 \mathrm{~cm}^{-1}$ ] lie slightly below those calculated for the Y- and L-isomers (166 and $186 \mathrm{~cm}^{-1}$, respectively), but above that calculated for the T-isomer ( $130 \mathrm{~cm}^{-1}$ ). These results appear to be consistent with our spectral assignment that the vibrationally excited levels ( $v_{4} \geq 4$ ) of $\mathrm{C}_{3}-\mathrm{Xe}$ act like those of a linear molecule. Unfortunately, the assignments of the vibrational levels below $329 \mathrm{~cm}^{-1}$ (above the zero-point energy level) are subject to uncertainty, since we do not know if they belong to the linear or the T-isomer. This can be seen in Table IV, which lists all the observed energy levels and our tentative assignments of the Xe complex from our wavelength-resolved emission spectra.

The vdW stretching frequency of the $\mathrm{C}_{3}-\mathrm{Xe}$ complex has been estimated as in Sec. IV for the $\mathrm{C}_{3}-\mathrm{Kr}$ complex. The resulting estimates for the T-, Y- and L-isomers are 50,40 , and $37 \mathrm{~cm}^{-1}$ for $v_{4} \geq 4$. From our calculation, the anharmonicity constants, $x_{i i}$, of the three isomers are the same to within $0.2 \mathrm{~cm}^{-1}$, being in the range -1.0 to $-1.2 \mathrm{~cm}^{-1}$. When the $\mathrm{C}_{3}$ molecule is nearly linear, the properties of the T - and Y-isomers become al-
most the same, and the vdW stretching frequency of the Y-isomer approaches the value of $50 \mathrm{~cm}^{-1}$. Since the observed vibrational levels of the Xe complex from our emission spectra are high vibrational levels, the structure should be more like the Y-isomer. Hence the observed vdW stretching frequency should be about $40 \mathrm{~cm}^{-1}$.

Figure 11 shows that the potential surface is almost flat in the region from $\phi=220^{\circ}$ to $320^{\circ}$, when R is greater than about $4.6 \AA$. The vdW bending frequency is therefore expected to become smaller when $v_{4} \geq 4$. Two low frequencies, $7-10$ and $12-18 \mathrm{~cm}^{-1}$ have been identified, as shown in Table IV. The latter seems to be twice the former. Since higher levels of the $\mathrm{C}_{3}-\mathrm{Xe}$ complex with $v_{4} \geq 4$ appear to behave like those of a linear molecule, the two vdW bending motions can be treated as a degenerate vibration ( $\nu_{5}$ ) with $\pi$ symmetry. We therefore expect to observe progressions in even quanta of $\nu_{5}$ in the emission spectra. Hence we assign the low frequency, $7-10 \mathrm{~cm}^{-1}$, as the ground state vdW bending frequency of the complex.

The emission spectrum from the vdW band of $\mathrm{C}_{3}-\mathrm{Xe}$ at $25015.5 \mathrm{~cm}^{-1}$ shows mostly transitions to the odd-numbered


FIG. 11. Contour plot of the calculated $\operatorname{CCSD}(\mathrm{T})$ energy of the $\mathrm{C}_{3}-$ Xe complex versus out-of-plane $\mathrm{C}_{3}$-bending angle, $\theta$, and in-plane vdW bending angle, $\phi$, at $\rho=112^{\circ}$ and fixed vdW bond length, $\mathrm{R}=4.8 \AA$. Contours are given for every $2 \mathrm{~cm}^{-1}$ from 626 to $676 \mathrm{~cm}^{-1}$; for energies above $680 \mathrm{~cm}^{-1}$, contours are shown for every $5 \mathrm{~cm}^{-1}$.
levels of $\nu_{5}{ }^{\prime \prime}$, which are forbidden transitions. This may explain the weakness of the LIF spectrum. Instead, two other nearby bands at 25004.7 and $25026.6 \mathrm{~cm}^{-1}$ have emission down to the even-numbered levels of $v_{5}{ }^{\prime \prime}$. On the other hand the levels at $25406.6,25430.9$ and $25516.7 \mathrm{~cm}^{-1}$ emit to the odd- and even-numbered levels of both $\nu_{4}{ }^{\prime \prime}$ and $\nu_{5}{ }^{\prime \prime}$. Since the Xe-complex appears to behave as a linear molecule in the $\tilde{A}$ state and in the levels of the $\tilde{X}$ state with $v_{4} \geq 4$, transitions are only expected to even quanta of $\nu_{4}$ or $\nu_{5}$ in the absence of vibronic coupling. Extensive $\nu_{5}{ }^{\prime \prime}$-progressions were also observed in the emission spectra from the vdW bands with $v_{4}{ }^{\prime}=2^{+}$and $4^{-}$. Hence, as for the Ã state, various frequency intervals in the range of $10.3-12.0 \mathrm{~cm}^{-1}$ appearing in the excitation spectra of the Xe-complex are assigned as single quanta of the vdW bending vibration of the A state.

## VII. DISCUSSION

Although some LIF spectra of the $\mathrm{C}_{3}-\mathrm{Kr}$ complex have been recorded at higher resolution, $\sim 0.06 \mathrm{~cm}^{-1}$, this is unfortunately not sufficient to resolve the rotational structure. Since the experimental conditions used to generate the $\mathrm{Ar}, \mathrm{Kr}$, and Xe complexes are very similar and the Ar complex is known
to be a $1: 1$ complex, ${ }^{10}$ we presume that the Kr and Xe complexes observed in this work are also 1:1 complexes.

No direct experimental information about the geometries of the Kr and Xe complexes at equilibrium is available yet, but we assume that they are also T-shaped, like the Ar complex, for which the structure was determined from our previous higher resolution LIF spectra. ${ }^{10}$ The wavelength-resolved emission spectra and the LIF excitation spectra of the Kr complex show considerable resemblance to those of the Ar complex, which leads us to believe that the Kr complex is T-shaped in both its $\tilde{X}$ and $\tilde{A}$ states; this is consistent with our $a b$ initio calculation of its ground electronic state structure.

The $a b$ initio calculations of the Xe complex showed that the T-/Y-shape will be its equilibrium structure, but at $v_{\mathrm{b}}$ (or $v_{4}$ ) $\geq 4$, an L-isomer becomes increasingly stable. Examination of the MOs calculated by the Hartree-Fock self-consistent field method indicates that the L-isomer of the Xe complex is stabilized by the mixing of some $\pi^{*}$ or $\sigma^{*}$ character into the $1 \pi_{\mathrm{u}}$ orbital. The $\tilde{\mathrm{A}}^{1} \Pi_{u}$ state, lying at $24675.6 \mathrm{~cm}^{-1},{ }^{12,13,16}$ is known to have the configuration $\ldots\left(2 \sigma_{\mathrm{u}}\right)^{1}\left(1 \pi_{\mathrm{u}}\right)^{4}\left(1 \pi_{\mathrm{g}}\right)^{1},{ }^{28-30}$ while the $\tilde{\mathrm{B}}^{1} \Sigma_{u}^{-}$and $\tilde{\mathrm{B}}^{\prime 1} \Delta_{u}$ states from the configuration $\ldots\left(2 \sigma_{\mathrm{u}}\right)^{2}\left(1 \pi_{\mathrm{u}}\right)^{3}\left(1 \pi_{\mathrm{g}}\right)^{1}$ lie at about $29500 \mathrm{~cm}^{-1} .{ }^{28-30}$ The $\tilde{\mathrm{B}}$ and $\tilde{\mathrm{B}}^{\prime}$ states are predicted to cross the $\tilde{A}$ state at an elongated $\mathrm{C}-\mathrm{C}$ bond length, $\sim 1.42 \AA$. Hence, it is very likely that the $\tilde{A}$ state of the Xe complex has
only a small potential barrier between the T- and L-shapes to account for the quick conversion from T to L within the fluorescence lifetime ( $\sim 200 \mathrm{~ns}$ ) of the $\tilde{A}$ state. This could perhaps have been anticipated because the electron distributions in the $\tilde{\mathrm{A}}, \tilde{\mathrm{B}}$, and $\tilde{\mathrm{B}}^{\prime}$ excited electronic states stabilize the L-shaped Xe complex. It could also be tested by examining the excitation spectra of the Xe complex near higher vibrational levels of the $\tilde{A}$ state. The vibrational assignments of the high vibrational levels of the $\tilde{A}$ state of $\mathrm{C}_{3}$, and a search for the $\tilde{\mathrm{B}}$ and $\tilde{\mathrm{B}}^{\prime}$ states, are in progress in our laboratory. ${ }^{31}$ It is hoped that we can address this question in the near future.

The emission spectra from the $2^{4-}$ and $2^{2+}$ levels of $\mathrm{C}_{3}(\tilde{\mathrm{~A}})$ down to the bending levels with $\mathrm{E}_{\text {vib }} \leq 1000 \mathrm{~cm}^{-1}$ were found to be very similar to each other, ${ }^{10}$ as might be predicted from the strong mixing caused by the orbital angular momentum. ${ }^{17}$ For the $\mathrm{C}_{3}-\mathrm{Ar}$ complex it was found ${ }^{10}$ that the vdW levels near the energy of the $\mathrm{C}_{3}, 2^{2+}$ level emit more strongly to even $v_{\mathrm{b}}$ levels of the ground electronic state than to odd ones; however, contrary results were observed from those near the $\mathrm{C}_{3}, 2^{4-}$ level. Similar patterns are found for the Kr and Xe complexes, as can be seen in Tables II and III. These results indicate that the Rg atom has a nonnegligible effect on the orbital angular momentum of the $\tilde{A}$ state.

The binding energies of the Kr and Xe complexes are estimated to be 280 and $300 \mathrm{~cm}^{-1}$, respectively, from $\operatorname{CCSD}(\mathrm{T}) /$ aug-cc-pVTZ calculations at their equilibrium geometries. The calculations also predict that the binding energy of the T -isomer increases as the $\mathrm{C}_{3}$ bending quantum number increases. The magnitudes of the red-shifts from the free $\mathrm{C}_{3}$ transitions, listed in Table I, allow us to estimate that the binding energies of the $\tilde{A}$ states of these two complexes lie in the ranges $302-318$ and $334-336 \mathrm{~cm}^{-1}$.

## VIII. CONCLUSIONS

Bands of the $\tilde{\mathrm{A}}-\tilde{\mathrm{X}}$ electronic transitions of the $\mathrm{C}_{3}-\mathrm{Kr}$ and $\mathrm{C}_{3}-\mathrm{Xe}$ complexes have been discovered accompanying bands of the $\tilde{\mathrm{A}}-\tilde{\mathrm{X}}$ system of the free $\mathrm{C}_{3}$ molecule, though not the $(0,0)$ band itself. No predissociations were detected in the $\tilde{A}$ states of the Kr and Xe complexes. Our experimental observations lead to the conclusion that both the upper and lower electronic states of the Kr complex are T -shaped. The $\mathrm{C}_{3}$-bending vibrational levels of the Kr complex are lower in energy than those of free $\mathrm{C}_{3}$ because of dipole-induced dipole interaction between the Kr atom and $\mathrm{C}_{3}$ in its higher bending levels. The energy lowerings observed for the Kr complex are larger than those found for the Ar complex, reflecting the larger polarizability of Kr . A simple perturbed harmonic oscillator model based on dipole-induced dipole interaction roughly reproduces the $\mathrm{C}_{3}$-bending vibrational levels of the Kr complex, with the interaction potential taken as $\mathrm{V}_{2} \cos 2 \theta$, where $V_{2}=6.3 \mathrm{~cm}^{-1}$.

Neglecting the large amplitude motion and anharmonicities, the vibrational frequencies of the ground electronic state of $\mathrm{C}_{3}-\mathrm{Kr}$ were determined to be $\nu_{2}=111(7), \nu_{3}(\mathrm{vdW}$ stretch $)$ $=37(2), v_{4}=40(3)$, and $v_{6}(\mathrm{vdW}$ bend $)=8(2) \mathrm{cm}^{-1}$.

Emission spectra from the $\tilde{A}, b^{2-}$ levels of the $\mathrm{C}_{3}-\mathrm{Xe}$ complex give evidence that a linear isomer of the complex becomes observable when four or more quanta of the $\mathrm{C}_{3}$ bending vibration are excited. The vibrational frequencies of this L-isomer of the ground electronic state of the Xe complex were found to be $\nu_{3}(\mathrm{vdW}$ stretch $)=42(3), \nu_{4}\left(\mathrm{C}_{3}\right.$-bending $)$ $=76(9)$, and $v_{5}(\mathrm{vdW}$ bend $)=8.5(15) \mathrm{cm}^{-1}$.

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[^0]:    ${ }^{\text {a Band }} \mathrm{A}$ of Fig. 3.
    ${ }^{\text {a Band A of Fig. }}$
    ${ }^{\mathrm{b}^{\text {Band }} \text { B of Fig. }}$
    ${ }^{\text {chand C of Fig. }}$
    ${ }^{1}$ Band $D$ of Fig. 3 .
    ${ }^{〔}$ Band E of Fig. 4
    ${ }^{\text {B }}$ Band G of Fig. 4.
    ${ }^{1}$ Band H of Fig. 5 .
    Band J of Fig. 5
    ${ }^{\prime} \nu_{1}$ and $\nu_{5}$ are the symmetric and antisymmetric C-C stretching vibrations, $\nu_{2}$ and $\nu_{4}$ are the in-plane and out-of-plane $\mathrm{C}_{3}$-bending vibrations, and $\nu_{3}$ and $\nu_{6}$ are the vdW stretching and bending vibrations. ${ }^{{ }_{m}}$ Broad line.

